

# ANALYZING VIRTUAL MATH TEAMS ENACTING GEOMETRIC PRACTICES

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## **Background of Data**

- Virtual Math Teams (VMT) with GeoGebra: online chat collaborative problem solving and dynamicgeometry construction environment
- 3 girls in same 7<sup>th</sup> grade algebra class (about 13 years old); 8 one-hour sessions after school
- Ch 7 in Translating Euclid
- Chat log excerpts in slides
- Complete log excerpts, can be filtered for chat, etc.
- Replayer files & replayer for 8 cereal-girls sessions

#### **Data Session**

- 1. Discuss background of data
- 2. Quickly go through data from topic 1 to get a feel of how the students started in VMT as a team
- 3. Look at data from "high point" where they solved a hard problem and demonstrated understanding of dynamic-geometry dependencies (topics 5 & 6)
- 4. Consider in more detail the discourse in the final section about constraints & dependencies (topic 13)











## Move Drag or select objects (Esc)





Welcome to GeoGebra for Virtual Math Teams!

Collaborate -- Take turns -- Make sure everyone agrees

\*\*\*Explore Points and Segments in Dynamic Geometry\*\*\*

- 1. Use chat to decide who will do each step.
- Someone click on the 'Take Control' button.
- 3. Click on the button for the Point tool at the top.
- 4. Now click a couple places to create some Points.
- Release control. Let someone else take control.
- 6. Click on the Move tool arrow on the left.
- 7. With this Move tool, click on a Point and drag it.
- 8. Someone select the next tool, the Line Segment Tool.
- 9. Click on two existing Points or two other places -- to construct a line Segment between the points.
- 10. Switch back to the Move tool to drag the Segment.
- 11. Everyone explore these tools in the tool bar.
- 12. Chat about what you notice.

When you are finished working together in one tab, move to the next. Try to finish all the tabs.

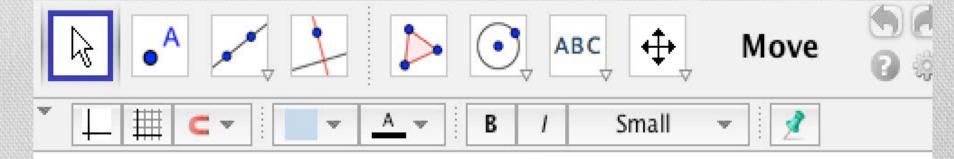
Line	Start Time	Post Time	Duration	Event Typ-T	User	Message
1		11:46.7	0:00:00	system	cornflakes	joins the room
2		12:45.3	0:00:58	system	fruitloops	joins the room
3	13:38.8	13:39.4	0:00:00	chat	cornflakes	hey
4	13:55.4	13:57.0	0:00:01	chat	fruitloops	hello
5		14:04.6	0:00:07	system	cheerios	joins the room
6	14:18.0	14:19.1	0:00:01	chat	cheerios	hey
7	14:39.4	14:45.6	0:00:06	chat	cheerios	whose froot loops
8	14:51.5	14:53.9	0:00:02	chat	cornflakes	daniella\
9	15:04.5	15:10.8	0:00:06	chat	cheerios	whose takimg control
10	15:15.5	15:20.1	0:00:04	chat	cheerios	taking*
11		15:38.5	0:00:18	system	cornflakes	Now viewing tab Hints Help
12		15:38.5	0:00:00	system	cornflakes	Now viewing tab Objects
13		15:41.1	0:00:02	system	cornflakes	Now viewing tab Dragging
14		15:42.6	0:00:01	system	cornflakes	Now viewing tab Constructing
15		15:45.4	0:00:02	system	cornflakes	Now viewing tab Dependencies
16		15:46.8	0:00:01	system	cornflakes	Now viewing tab Welcome
17		15:59.6	0:00:12	system	cornflakes	Now viewing tab Hints Help
18		16:08.0	0:00:08	system	cornflakes	Now viewing tab Objects
19	16:11.5	16:18.4	0:00:06	chat	cheerios	so whoses doing what
20		16:14.8	0:0:-3	system	cornflakes	Now viewing tab Hints Help
21		16:17.7	0:00:02	system	cornflakes	Now viewing tab Welcome
22	16:32.5	16:44.4	0:00:11	chat	fruitloops	who wants to take control?
	16:49.7	16:57.7	0:00:08	awareness	fruitloops	[fully erased the chat message]
	17:05.7	17:19.1	0:00:13	awareness	cornflakes	[fully erased the chat message]
23	17:24.7	17:30.6	0:00:05	chat	cheerios	daniella do you want to

21		16:17.7	0:00:02	system	cornflakes	Now viewing tab Welcome
22	16:32.5	16:44.4	0:00:11	chat	fruitloops	who wants to take control?
	16:49.7	16:57.7	0:00:08	awareness	fruitloops	[fully erased the chat message]
	17:05.7	17:19.1	0:00:13	awareness	cornflakes	[fully erased the chat message]
23	17:24.7	17:30.6	0:00:05	chat	cheerios	daniella do you want to
	17:37.5	17:39.9	0:00:02	awareness	fruitloops	[fully erased the chat message]
24	17:40.7	17:52.2	0:00:11	chat	fruitloops	no cornflakes you take controll
25	17:55.1	18:01.7	0:00:06	chat	fruitloops	who wants to do what steps?
26	17:55.4	18:02.9	0:00:07	chat	cheerios	cornflakes take control
27	17:57.8	18:03.6	0:00:05	chat	cornflakes	no cheerios you can
28	18:06.2	18:14.6	0:00:08	chat	cheerios	cornflakes
	18:16.8	18:18.2	0:00:01	awareness	cheerios	[fully erased the chat message]
29	18:21.5	18:25.4	0:00:03	chat	fruitloops	cornflakes
30	18:33.0	18:33.6	0:00:00	chat	cornflakes	NO
31	18:37.8	18:40.0	0:00:02	chat	cheerios	why not
32	18:44.0	18:52.3	0:00:08	chat	fruitloops	i just took control. lets takes turns
33	18:56.1	19:01.9	0:00:05	chat	cheerios	alright
34	19:02.5	19:03.0	0:00:00	chat	cornflakes	ok
35	19:19.8	19:26.6	0:00:06	chat	cheerios	it says no one has control
36	19:25.1	19:30.1	0:00:04	chat	fruitloops	what do we do know?
37	19:35.3	19:44.3	0:00:08	chat	cheerios	i am not sure cornflakes do u know
	20:02.7	20:03.3	0:00:00	awareness	cheerios	[fully erased the chat message]
38	20:03.6	20:17.4	0:00:13	chat	cheerios	i think we have to follow the numbered list
39	20:17.1	20:20.0	0:00:02	chat	cornflakes	uh mo
	20:20.1	20:22.1	0:00:02	awareness	cheerios	[fully erased the chat message]
40	30.34 3	3U-36 V	0.00.14	chat	choorios	so lots do that and we will figure it out as we go

38	20:03.6	20:17.4	0:00:13	chat	cheerios	i think we have to follow the numbered list
39	20:17.1	20:20.0	0:00:02	chat	cornflakes	uh mo
	20:20.1	20:22.1	0:00:02	awareness	cheerios	[fully erased the chat message]
40	20:24.2	20:38.4	0:00:14	chat	cheerios	so I ets do that and we will figure it out as we go
41	20:45.0	20:50.6	0:00:05	chat	fruitloops	someone else take control for now
42	20:46.8	20:53.1	0:00:06	chat	cheerios	lets*
43	21:02.3	21:17.5	0:00:15	chat	fruitloops	just follow the welcome thing
	21:05.0	21:09.9	0:00:04	awareness	cheerios	[fully erased the chat message]
	21:14.3	21:19.9	0:00:05	awareness	cheerios	[fully erased the chat message]
	21:19.9	21:24.1	0:00:04	awareness	cheerios	[fully erased the chat message]
44	21:24.8	21:32.9	0:00:08	chat	cheerios	yeah so we are on #3
45	21:48.7	21:56.2	0:00:07	chat	cornflakes	ok someoen else take control
	21:55.3	21:59.4	0:00:04	awareness	fruitloops	[fully erased the chat message]
46	22:00.4	22:05.3	0:00:04	chat	fruitloops	someone take control
47	22:05.0	22:13.1	0:00:08	chat	cheerios	whats happening?
48	22:18.2	22:18.7	0:00:00	chat	fruitloops	idk
	22:21.3	22:25.0	0:00:03	awareness	cheerios	[fully erased the chat message]
49	22:27.1	22:30.8	0:00:03	chat	cheerios	i am so lost
50	22:29.2	22:36.6	0:00:07	chat	fruitloops	i took control. what should i do?
51	22:40.1	22:42.3	0:00:02	chat	cornflakes	make a line
52	22:40.8	22:50.9	0:00:10	chat	cheerios	i am not sure #3 i guess?
53	23:01.9	23:10.4	0:00:08	chat	cornflakes	no i already did 3, do 5
54	23:05.4	23:10.5	0:00:05	chat	fruitloops	okay now what?
55	23:40.3	24:02.8	0:00:22	chat	cheerios	it says to release control
56	23:42.9	23:43.6	0:00:00	chat	cornflakes	good
57	32.45 5	24.177	0.00.33	chat	fruitlance	now compone orice continue

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54	23:05.4	23:10.5	0:00:05	chat	fruitloops	okay now what?
55	23:40.3	24:02.8	0:00:22	chat	cheerios	it says to release control
56	23:42.9	23:43.6	0:00:00	chat	cornflakes	good
57	23:45.5	24:17.7	0:00:32	chat	fruitloops	now someone erlse continue
58	24:05.2	24:12.8	0:00:07	chat	cheerios	and then do #6
59	24:11.5	24:15.7	0:00:04	chat	cornflakes	then release control
60	24:22.8	24:24.7	0:00:01	chat	fruitloops	released
61	24:24.7	24:29.0	0:00:04	chat	cornflakes	cheerios will
62	24:32.6	24:44.4	0:00:11	chat	fruitloops	take control and explore with the other toolos
63	24:51.3	24:57.3	0:00:05	chat	cheerios	i just did 6
64	25:14.0	25:17.5	0:00:03	chat	cornflakes	ill do 7 then
65	25:19.9	25:21.6	0:00:01	chat	cheerios	ok
66	25:25.2	25:26.1	0:00:00	chat	fruitloops	ok
67	25:39.9	25:51.0	0:00:11	chat	fruitloops	do likie 9 and 10 also
68	25:48.9	25:50.2	0:00:01	chat	cornflakes	ok done
	25:49.6	25:51.6	0:00:01	awareness	cheerios	[fully erased the chat message]
69	26:18.7	26:24.1	0:00:05	chat	cheerios	what about 8
	26:38.6	26:41.4	0:00:02	awareness	cheerios	[fully erased the chat message]
70	26:38.8	26:41.1	0:00:02	chat	fruitloops	yeah
71	26:45.5	26:51.1	0:00:05	chat	fruitloops	can i go next?
72	26:45.7	26:46.6	0:00:00	chat	cornflakes	there
73	26:54.9	26:57.3	0:00:02	chat	cornflakes	yeah go ahead
74	26:56.1	26:57.1	0:00:01	chat	cheerios	yes
75	27.07.6	27.14.1	0.00.06	chot	fruitlaana	Coursing plantage of the it?

100 100 100 100 100 100 100 100 100 100						
73	26:54.9	26:57.3	0:00:02	chat	cornflakes	yeah go ahead
74	26:56.1	26:57.1	0:00:01	chat	cheerios	yes
75	27:07.6	27:14.1	0:00:06	chat	fruitloops	so we just play around with it?
76	27:12.1	27:19.9	0:00:07	chat	cheerios	now the triangle is bigger
77	27:17.6	27:22.0	0:00:04	chat	cornflakes	i guess pretty much
78	27:30.1	27:35.5	0:00:05	chat	cheerios	are we on 11
79	27:35.1	27:44.5	0:00:09	chat	fruitloops	how do we get the line to connect to the piont?
80	27:39.2	27:41.0	0:00:01	chat	cornflakes	yes mam
81	27:44.7	27:45.2	0:00:00	chat	cheerios	kk
82	27:58.2	28:00.0	0:00:01	chat	fruitloops	nevermind
83	28:09.1	28:12.7	0:00:03	chat	cheerios	what now?
84	28:20.3	28:27.9	0:00:07	chat	cornflakes	chat about whatr we njotice?
85	28:32.2	28:41.6	0:00:09	chat	cheerios	well its a very interestiong shape
	28:34.8	28:38.9	0:00:04	awareness	fruitloops	[fully erased the chat message]
86	28:42.6	29:04.0	0:00:21	chat	cheerios	a rectangle and a triangle thats mushed together
87	28:48.5	29:10.8	0:00:22	chat	cornflakes	its like a polygon
88	29:13.0	29:14.8	0:00:01	chat	cornflakes	right?
				chat	cornflakes	no curved edges cause its made of a line segment
						and line segments are lines and lines that dont
89	29:15.3	29:38.5	0:00:23			have curves
90	29:18.6	29:22.5	0:00:03	chat	cheerios	it has 6 sides
91	29:26.9	29:40.1	0:00:13	chat	cheerios	and obtuse and acute angles no right angles
92	29:29.9	29:34.6	0:00:04	chat	fruitloops	how do i make it smaller?
				chat	cornflakes	yuppies no right angles
93	29:50.3	29:57.4	0:00:07			
94	29:54.9	29:58.9	0:00:04	chat	fruitloops	should we move on?
95	30:01.7	30:03.5	0:00:01	chat	cornflakes	yessiree
96	30:02.1	30:11.3	0:00:09	chat	cheerios	i think we should
97		30:07.4	0:0:-3	system	cornflakes	Now viewing tab Hints Help
98		30:12.8	0:00:05	system	cheerios	Now viewing tab Hints Help
99	30:13.1	30:16.0	0:00:02	chat	fruitloops	okay lets go
100		30:18.6	0:00:02	system	fruitloops	Now viewing tab Hints Help
CHARLES AND ALCOHOLOGY	7. VILTO, RUNE BY, PUBLISH BY THE THE BY THE REST.	ne the throne points the throne to the throne	<b>电阻电阻阻电电阻电阻电阻电阻</b>	THE THE THE PART HE THE THE THE THE THE THE THE THE THE	COLUMN TO THE TREAT THE TR	

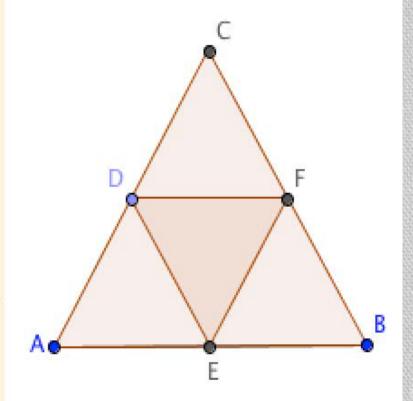


Take turns dragging vertex A of Triangle ABC and vertex D of Triangle DEF.

Chat about dependencies you notice and what you wonder about this figure.

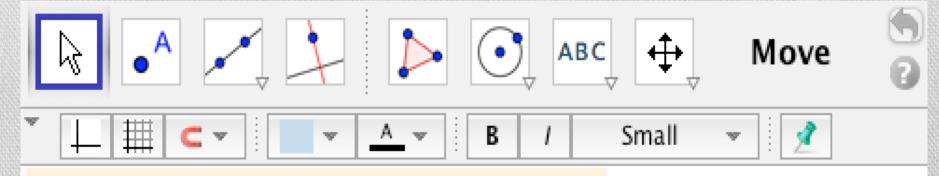
Construct a triangle inscribed in a triangle that behaves the same as this one. Chat about how you are constructing and why.

It might be helpful to look at the other tabs for this Topic and think about them together.



66	18:05.3	18:30.0	0:00:24	chat	cheerios	as i was movign d segment da is the same distance as segment be
	18:29.1	18:33.7	0:00:04	awareness	cornflakes	[fully erased the chat message]
67	18:45.8	18:52.0	0:00:06	chat	cheerios	and also cf
68	19:25.6	19:41.6	0:00:16	chat	cheerios	our kg is the same as ad
	19:45.1	19:49.4	0:00:04	awareness	cornflakes	[fully erased the chat message]
69	20:04.2	20:06.3	0:00:02	chat	cornflakes	agrreeed
70	20:04.5	20:06.5	0:00:02	chat	fruitloops	i agree
	20:38.1	20:39.1	0:00:00	awareness	cheerios	[fully erased the chat message]
				chat	cheerios	there should be a point on segment gh which is the same distance as kg and
71	20:39.6	21:21.8	0:00:42			also between segment uh
72	21:54.9	22:00.5	0:00:05	chat	cheerios	it should be ih not uh
				chat	cheerios	so i used the compass tool and measured kg and used point i as the center
73	23:12.2	23:39.9	0:00:27			and created a circle

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90	16:11.8	16:18.2	0:00:06	chat	cheerios	we have to explain what we did
	17:44.5	17:45.5	0:00:00	awareness	cornflakes	[fully erased the chat message]
				chat	cheerios	so first u have to plot a random point on the triangle we used k . then i
91	17:49.2	19:49.0	0:01:59			realised the distance from kg is the same as im and rh
				chat	cheerios	then you have to use the compass tool in are case are the length of are radius
						is kg so then we clicked those 2 points and used vertex i as the center the way
						to plot are second point of are triangle is where the circle and segment ih
92	19:49.8	22:51.2	0:03:01			intersect
93	20:39.8	20:41.4	0:00:01	chat	cornflakes	right
94	22:52.0	23:53.2	0:01:01	chat	cheerios	and then we repeated that step with the other side and h was the center
95	23:35.4	23:48.8	0:00:13	chat	cornflakes	yes you had to make the point between the circles
96	24:04.9	24:21.0	0:00:16	chat	cheerios	not between the circles where the segment intersect with the circle
	24:22.3	25:37.0	0:01:14	awareness	fruitloops	[fully erased the chat message]
97	25:22.0	25:27.5	0:00:05	chat	cornflakes	yea same thing
98	25:40.7	26:04.4	0:00:23	chat	fruitloops	so then why are point m and r shaded dark and don tact the same as k
99	25:50.0	25:52.4	0:00:02	chat	cheerios	its differnt
100	25:54.5	25:58.5	0:00:04	chat	cheerios	different*
101	25:56.1	26:00.0	0:00:03	chat	cornflakes	yes i know
102	26:09.9	26:14.6	0:00:04	chat	cheerios	they are restricted
103	26:32.3	26:35.6	0:00:03	chat	fruitloops	but whyy??????
104	26:35.9	26:45.8	0:00:09	chat	cornflakes	yeah if its a darker its restricted i think
105	26:49.6	26:52.1	0:00:02	chat	cheerios	yes
106	26:54.4	26:56.4	0:00:02	chat	cheerios	correct
107	28:13.9	28:31.0	0:00:17	chat	fruitloops	but why are m and r restricted but k isnt?
10 mm m m m m m m m m m m m m m m m m m	30:08.5	30:24.7	0:00:16	awareness	cheerios	[fully erased the chat message]
108	30:24.0	30:33.3	0:00:09	chat	cornflakes	because the invisible cirlcels are still there
				chat	fruitloops	okay so its because we made k by just using the point tool and putting it on
1000 1000 1000 1000 1000 1000 1000 100						the line but with m and r we maade it through using circles so technicaly, the
109	30:25.7	31:35.0	0:01:09			circle is still there but its hidden but we just dont see it.



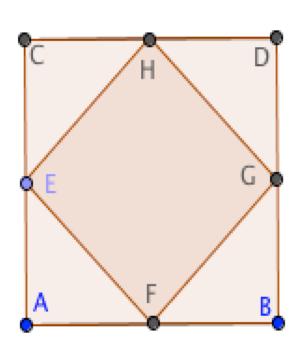
Take turns dragging vertex A of Quadrilateral ABDC and vertex E of Quadrilateral EFGH.

Chat about dependencies you notice and what you wonder about this figure.

Construct a Quadrilateral inscribed in a Quadrilateral that behaves the same as this one.

Chat about how you are constructing and why.

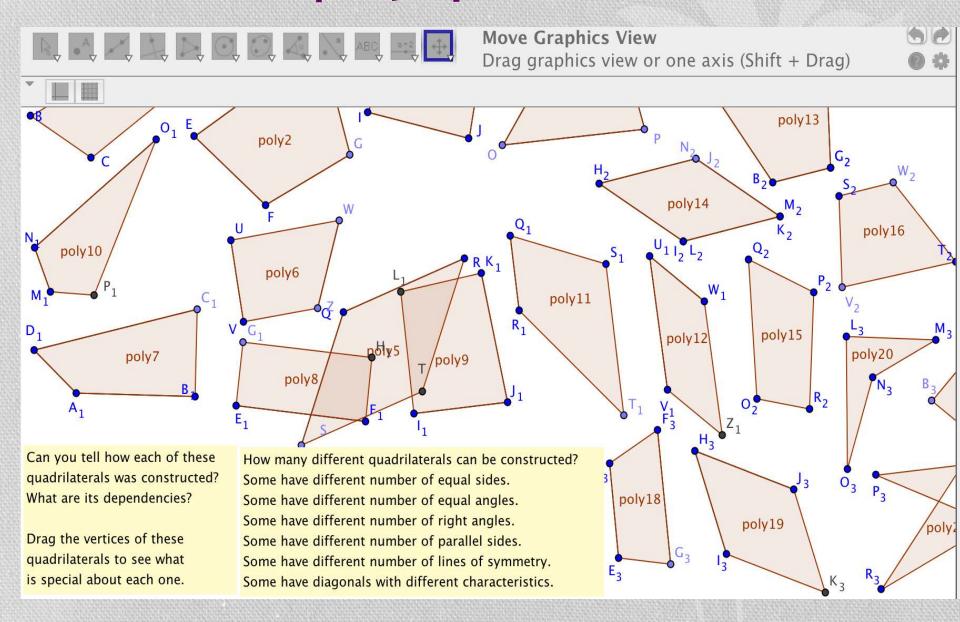
Note that the Compass tool is available by pulling it down from the Circle tool in the tool bar.



123	35:31.6	35:34.3	0:00:02	chat	cornflakes	E IS RESTRICTED
124	35:33.0	35:58.6	0:00:25	chat	fruitloops	do how do we create a square like the outer square?
125	36:42.1	36:54.4	0:00:12	chat	cheerios	we have to talk about the dependencies and stuff
126	36:55.8	37:01.3	0:00:05	chat	cheerios	read the instructions
127	37:28.5	38:45.9	0:01:17	chat	fruitloops	how but how do we make the square?
	38:55.0	38:56.3	0:00:01	awareness	fruitloops	[fully erased the chat message]
128	38:57.2	39:11.6	0:00:14	chat	fruitloops	like i know how to make the triangle but now the square
129	39:10.2	39:11.5	0:00:01	chat	cheerios	a grid
130	39:10.2	39:20.3	0:00:10	chat	cornflakes	olets start by cinstructing a regular square
131	39:15.2	39:16.5	0:00:01	chat	cheerios	a grid
	39:24.8	39:32.6	0:00:07	awareness	fruitloops	[fully erased the chat message]
132	39:33.4	39:48.0	0:00:14	chat	fruitloops	i think we should make perpendicular lines somehow
133	39:52.4	39:58.8	0:00:06	chat	cheerios	use the perpindicular line tool
134	43:13.3	43:21.9	0:00:08	chat	fruitloops	the first line segment would be like ab
135	43:27.2	43:27.7	0:00:00	chat	cornflakes	yes
136		44:12.6	0:00:25	system	cheerios	Now viewing tab Triangles
137		44:35.4	0:00:01	system	cheerios	Now viewing tab Squares
138	51:14.2	51:24.7	0:00:10	chat	cheerios	how do u know ji is straight
139	55:26.3	55:40.6	0:00:14	chat	fruitloops	i dont know what to do because the points arent the same color
140	56:26.0	56:38.2	0:00:12	chat	fruitloops	now after you make the perpendicular lines try to make the circles\
141	57:35.8	57:48.7	0:00:12	chat	fruitloops	i think you need to know use the polygon tool and make the square
				chat	cheerios	i made a line segment which was if than i used the perpendicular line tool and
						made 2 lines on each side then used the compass tool and clicked on each
(1964) (1964) (1964) (1964) (1964) (1964) (1964) (1964)						point and then the center vertex was i and then made a another circle except
142	58:50.9		0:01:51			the center vertex is j and connected all the points
Stanton and Stanton		na a sana a			ON THE COMMENT OF THE PROPERTY OF THE COMMENT OF TH	

A STATE OF THE PARTY OF THE PARTY.	CALTERNATION FOR THE TAX THE TAX THE THE THE THE	PARTY AND RESIDENCE AND PROPERTY OF ANY	CA PROPERTY DE PROPERTY DE LA VIANO			
143	58:51.5	59:10.6	0:00:19	chat	fruitloops	now we need to use the compass tool lilke we did in the triangles tab
144	59:38.3	59:57.5	0:00:19	chat	fruitloops	because af is equal to ec and dh and bc
145	00:57.6	01:15.3	0:00:17	chat	cheerios	then used to polygon tool and then hid the circles and lines
146	01:05.1	01:07.5	0:00:02	chat	fruitloops	correct
				chat	fruitloops	and we used the circles to make the sides equal because the sides are their
147	01:08.7	01:36.9	0:00:28			radius
148	02:29.8	02:39.8	0:00:09	chat	fruitloops	point m is like point e because it moves around
149	02:44.2	02:48.8	0:00:04	chat	fruitloops	and its the same color
150	04:11.6	04:14.4	0:00:02	chat	fruitloops	good!!
151	04:36.3	04:40.4	0:00:04	chat	fruitloops	now hide the circles
152	05:16.7	05:25.7	0:00:09	chat	fruitloops	the points match up
153	05:30.2	06:00.8	0:00:30	chat	fruitloops	it works! just like the original circl;e
154	05:39.5	05:47.2	0:00:07	chat	cheerios	yay it works
				chat	cheerios	so just plotted a random point on line segment jk and then used the compass
						tool and clicked on point m and j ( radius) and then clicked k to be the center
						and then plotted the point where line segment kl intersect with the circle and
155	07:10.5	09:42.5	0:02:32			repeated these steps on the other sides
				chat	fruitloops	i think points o, n, and p are dark because they weere made using the original
156	08:14.4	09:18.8	0:01:04			circles
157	08:22.9	08:23.8	0:00:00	chat	cornflakes	yess
158	09:26.1	09:32.4	0:00:06	chat	cornflakes	yea i agreeee
159	09:45.5	10:27.8	0:00:42	chat	cheerios	the distance between m and j is the same between ok and ln and pi
160	09:57.1	10:02.9	0:00:05	chat	fruitloops	yeah i saw and i understand
				chat	fruitloops	all the radii are the same so the distances from ko,ln, and ip and jm are the
161	10:03.7	10:45.0	0:00:41			same
162	10:16.3	10:18.5	0:00:02	chat	cornflakes	same
163	10:52.8	10:57.3	0:00:04	chat	cornflakes	yup i agrree
164	10:59.3	11:01.3	0:00:02	chat	cheerios	yes
Charles to the page to	ONE NOTICE AND ADDRESS OF THE ADDRES	NACATAVATORA (NEASTAPAVA)	Carried to the facility the facility the facility			

### **Topic 13: Quadrilaterals**



100					•		-
13	3/11/13	14:52.6	15:00.2	0:00:07	chat	fruitloops	lets start with quad abcd
14	3/11/13	15:06.6	15:18.5	0:00:11	chat	fruitloops	in the upper lefthand corner
15	3/11/13	15:47.0	15:47.4	0:00:00	chat	cornflakes	ok
					chat	fruitloops	okay so for poly 1 all the points can
							move anywhere and i dont think they
16	3/11/13	15:54.1	16:26.5	0:00:32			have resrictions
17	3/11/13	16:06.7	16:20.1	0:00:13	chat	cheerios	label it by saying its points
18	3/11/13	16:41.9	16:42.3	0:00:00	chat	cornflakes	ok
					chat	fruitloops	so i think this was constructed by just
							making four points and using a polygon
19	3/11/13	16:47.2	17:19.1	0:00:31			tool
20	3/11/13	17:29.5	17:38.1	0:00:08	chat	fruitloops	you guys can try moving if youd like
					chat	cornflakes	yeah your right i dont think theres any
21	3/11/13	17:56.8	18:14.2	0:00:17			restrictions
22	3/11/13	18:17.1	18:23.2	0:00:06	chat	cheerios	can i try
23	3/11/13	18:50.6	19:00.7	0:00:10	chat	cheerios	there are no restrictions like you said
					chat	fruitloops	so do you agree with how i think it was
24	3/11/13	19:14.3	19:34.6	0:00:20			constructed
25	3/11/13	19:37.9	19:38.6	0:00:00	chat	cornflakes	yes
26	3/11/13	19:42.0	19:53.4	0:00:11	chat	fruitloops	okay good

					chat	cheerios	what si the difference between
44	3/11/13	24:01.0	24:16.7	0:00:15			constrained and restricted
45	3/11/13	24:22.1	24:24.3	0:00:02	chat	cheerios	is*
					chat	fruitloops	also when you move e, g moves away
46	3/11/13	24:23.3	24:46.4	0:00:23			or closer to f
47	3/11/13	24:35.0	24:41.6	0:00:06	chat	cornflakes	constrained is limited function
48	3/11/13	24:54.2	25:08.4	0:00:14	chat	fruitloops	so i think g it definitly constrained
49	3/11/13	25:13.2	25:14.0	0:00:00	chat	cornflakes	yes
50	3/11/13	25:16.1	25:19.8	0:00:03	chat	cornflakes	i think that too
51	3/11/13	25:23.4	25:25.6	0:00:02	chat	cheerios	why though
	2/11/12	25.26.5	25.50.2	0.00.22	chat	fruitloops	and g moves whenever you move point e and f but it doesnt move when you
52	3/11/13	25:36.5	25:59.3	0:00:22	<b>—</b>	6 111	move h
					chat	fruitloops	@ cheerios. i think its constrained
756 4 506 4 507 4 507 4 507 5 507	_ ,, , ,, _						because it moves but the function is
53	3/11/13	26:07.0	26:42.4	0:00:35			limited
54	3/11/13	26:17.7	26:20.3	0:00:02	chat	cheerios	okay
Control of the contro	3/11/13	26:44.4	27:04.9	0:00:20	awareness	fruitloops	[fully erased the chat message]
55	3/11/13	27:28.4	27:37.5	0:00:09	chat	fruitloops	what is the definition of dependant
56	3/11/13	27:33.3	27:36.8	0:00:03	chat	cheerios	oh i see
					chat	cheerios	u need the other line or point
57	3/11/13	28:38.0	28:52.4	0:00:14			otherwise it wont work
66 0 1976 04 0 1970 04 0 1870 1870					chat	fruitloops	do you guys have any idea of how this
58	3/11/13	28:43.6	28:54.6	0:00:10			was made?
59	3/11/13	28:57.1	29:15.6	0:00:18	chat	cornflakes	yeah some points are dependent on others
Control of the contro					chat	cornflakes	maybe some invisible circles and the shapes could be dependent on thos
<mark>60</mark>	3/11/13	29:23.4	29:43.4	0:00:19			circles

64	3/11/13	30:45.5	30:55.5	0:00:09	chat	fruitloops	i think it has to do with how it was constructed
					chat	fruitloops	cause eremember how before in the
							other topic we would sometimes use
							circles to construct stuff and then hide
							the circles? well maybe thiis quad was
65	3/11/13	30:57.4	31:44.4	0:00:47			made using a circle
	3/11/13	31:01.0	31:01.5	0:00:00	awareness	cheerios	[fully erased the chat message]
66	3/11/13	31:02.4	31:03.8	0:00:01	chat	cheerios	i agree
67	3/11/13	31:25.1	31:29.1	0:00:03	chat	cornflakes	YES
					chat	cornflakes	yeah and one of the points was on the
68	3/11/13	31:50.4	31:58.9	0:00:08			circle
					chat	cheerios	yeah that makes sense remember
							when we made the triangle the same
69	3/11/13	32:17.3	32:38.1	0:00:20			thing happened
70	3/11/13	32:42.3	32:43.0	0:00:00	chat	cornflakes	yes
					chat	fruitloops	but i dont really know how it could
71	3/11/13	33:00.4	33:10.4	0:00:10			have been made?
					chat	fruitloops	do you thinkk point e is the same
72	3/11/13	33:59.6	34:17.4	0:00:17			distance away from f as g?
					chat	cheerios	maybe they used another shape
73	3/11/13	34:03.8	34:14.5	0:00:10			instead of circles
					chat	cornflakes	we coulda had a shape on a triangle or
							square made it invisible but in reality
							the other shape is still there therefore
							making one of tth e points that was on
74	3/11/13	34:13.7	35:03.6	0:00:49			the shape dependent on that shape
					chat	cheerios	i think it is the same tool maybe they
							used the compass tool cuz they have
75	3/11/13	35:06.1	35:31.9	0:00:25			the same distance
76	3/11/13	36:02.3	36:13.9	0:00:11	chat	fruitloops	and h is just completely unrestriced
					chat	cornflakes	yeah it probably wasnt built on
77	3/11/13	36:21.3	36:30.8	0:00:09			anything
1010101010101	3/11/13	36:23.3	36:26.4	0:00:03	awareness	cheerios	[fully erased the chat message]

	3/11/13	36:23.3	36:26.4	0:00:03	awareness	cheerios	[fully erased the chat message]
78	3/11/13	36:26.9	36:31.7	0:00:04	chat	cheerios	agreed
79	3/11/13	36:36.2	36:37.6	0:00:01	chat	fruitloops	agreed
					chat	fruitloops	so h was probably the first point
80	3/11/13	36:38.5	36:55.4	0:00:16			construceted in building the shape
	3/11/13	36:54.1	37:02.3	0:00:08	awareness	cheerios	[fully erased the chat message]
81	3/11/13	37:03.1	37:05.9	0:00:02	chat	cheerios	yeah
	3/11/13	37:06.4	37:09.8	0:00:03	awareness	cheerios	[fully erased the chat message]
	3/11/13	37:09.4	37:20.7	0:00:11	awareness	fruitloops	[fully erased the chat message]
	3/11/13	37:11.3	37:13.4	0:00:02	awareness	cheerios	[fully erased the chat message]
82	3/11/13	37:11.5	37:14.9	0:00:03	chat	cornflakes	whatb do you mean?
					chat	fruitloops	well if h can move anywhere it was
							probably made first cause if you just
							put a random point anywhere it is the
							same dark blue color as h and it can
83	3/11/13	37:21.4	38:16.7	0:00:55			move anywhere
	3/11/13	37:24.4	37:25.0	0:00:00	awareness	cheerios	[fully erased the chat message]
84	3/11/13	37:25.2	37:33.2	0:00:07	chat	cheerios	the first point plotted?
85	3/11/13	37:41.7	37:51.7	0:00:09	chat	cornflakes	doesnt it go in alphabetical order?
86	3/11/13	38:02.4	38:06.7	0:00:04	chat	cornflakes	efg and then h
	3/11/13	38:03.1	38:10.5	0:00:07	awareness	cheerios	[fully erased the chat message]
					chat	cornflakes	but e and f are the same
87	3/11/13	38:28.9	38:45.0	0:00:16			color>>>>>>
88	3/11/13	38:51.1	39:02.3	0:00:11	chat	fruitloops	but e and f are constrained
89	3/11/13	39:06.0	39:14.6	0:00:08	chat	fruitloops	i dont know for sure maybe youre right
90	3/11/13	39:51.6	39:57.6	0:00:05	chat	cheerios	im not very sure either
91	3/11/13	40:00.5	40:02.4	0:00:01	chat	cornflakes	meneither
92	3/11/13	40:11.6	40:19.3	0:00:07	chat	cheerios	can i do the next polygon
93	3/11/13	40:15.2	40:21.9	0:00:06	chat	fruitloops	should we move on or??

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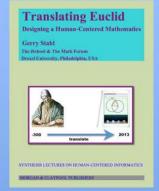


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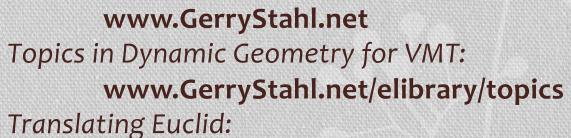
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